









Addition

In developing a written method for addition, it is important that children understand the concept of addition, in that it is:

- Combining two or more groups to give a total or sum
- Increasing an amount

They also need to understand and work with certain principles, i.e. that it is:

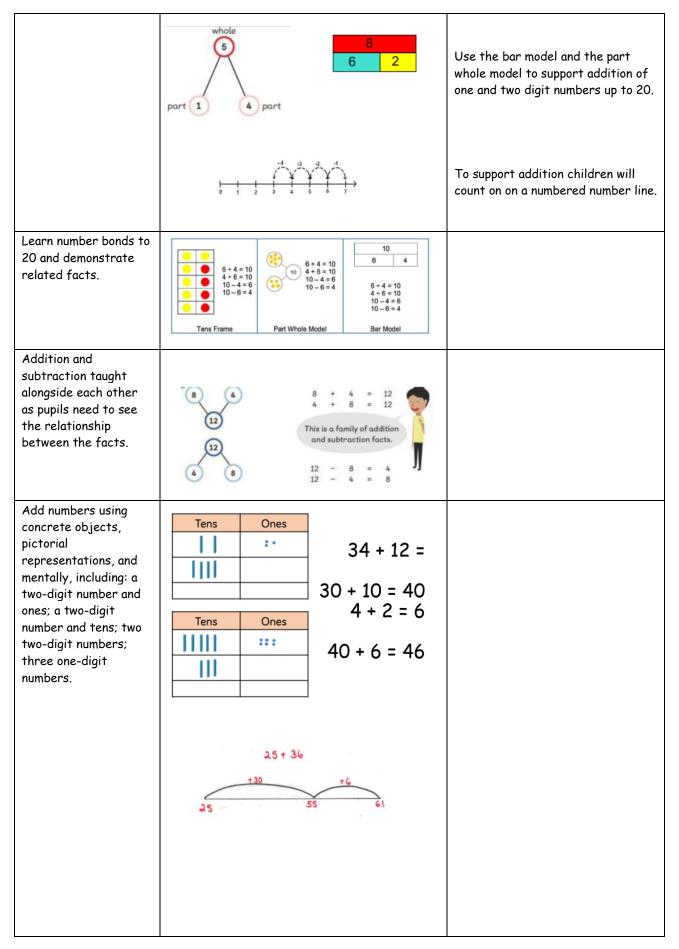
- the inverse of subtraction
- commutative i.e. 5 + 3 = 3 + 5
- associative i.e. 5 + 3 + 7 = 5 + (3 + 7)

The fact that it is commutative and associative means that calculations can be rearranged, e.g. 4 + 13 = 17 is the same as 13 + 4 = 17.

Expectation	Example	Additional Information
Using quantities and objects, children add two single-digit numbers and count on to find the answer.		Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of practical equipment, including small world play, role play, counters, cubes etc.
		At this stage, children will focus on a counting all method and then a counting on method.
	Number bonds to 10	i.e. Combining two parts to make a whole using concrete methods to support addition of single digit numbers.
	$ \begin{array}{r} 0 + 10 = 10 \\ 1 + 9 = 10 \\ 2 + 5 = 10 \\ 3 + 7 = 10 \\ 4 + 6 = 10 \\ 5 + 5 = 10 \\ 6 + 4 = 10 \\ \hline - 1 - 2 - 3 $	Solve problems using concrete and pictorial methods.
	7 + 3 = 10 $8 + 2 = 10$ $9 + 1 = 10$ $10 + 0 = 10$	Children will also be able to mentally Recall number bonds to 10.
Add one-digit and two- digit numbers to 20, including zero (using	3 + 4 = 7	Combining two parts to make a whole
concrete objects and pictorial representations).	5+2=7 2+4=6	Continuing to use concrete and pictorial methods to support addition, i.e. counters and ten frames (Joining two groups and then recounting all objects (lots of practice making 10 and numbers to 10 e.g. 6 + 4 = 10 or 3 + 5 = 8).











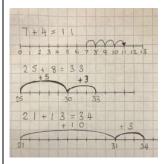
Add numbers with up to three digits, using formal written method of columnar addition.

Add numbers with up to 4 digits and decimals with one decimal place using the formal written method of column addition where appropriate.

Add whole numbers with more than 4 digits and decimals with two decimal places, including formal written methods (columnar addition).

Add whole numbers and decimals using formal written methods (columnar addition). - Need year 6 modelled example.

Stage 1



Step 2



Step 2 with decimals

4	.0	2	+	2	9	3	1,	6.	9	5	
+		.0	10235								
	3.	4	2	+	0,	7	7	0	4.	1	9
+	U. 3. 0. 4.	7	2 7								
	1		-								

Step 3

	1	2	7	+	1	1	2	=	2	3	9	
		T 2										
+	2	3 03	729009	000	+00	2,	1 +	0)	0	0)		
	1	4	8	+	1	3	7	t)	2	8	5	
+	#11/22	4317	0875005	(4	0	+	3	0)	0	0)		

Addition starts with adding on using a numbered number line (jumps above the number line) using mental 'counting on' strategies such as number bonds.

A similar method is used to develop this stage but on a blank number line.

This method relies on the children's knowledge of place value and mental addition strategies.

Stage 2 and 3 are the next stage of addition where formal written method is introduced where the children must have secure knowledge of place value.
Stage 3 is the final stage of addition with regular use of exchanging relying heavily on the children's knowledge of place value and adding multiples of 10 and 100.





Subtraction

In developing a written method for subtraction, it is important that children understand the concept of subtraction, in that it is:

- Removal of an amount from a larger group (take away)
- Comparison of two amounts (difference)

They also need to understand and work with certain principles, i.e. that it is:

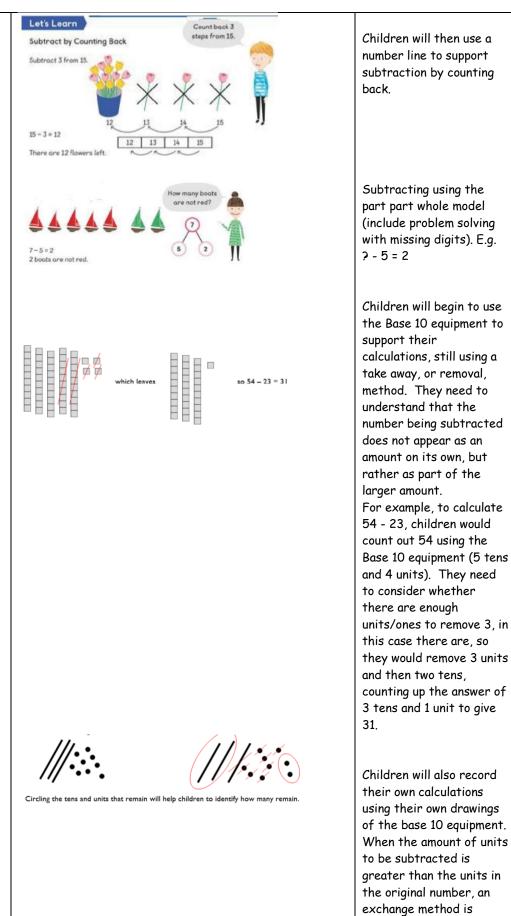
- the inverse of addition
- not commutative i.e. 5 3 is not the same as 3 5
- not associative i.e. 10 3 2 is not the same as 10 (3 2)

Example Additional Information Expectation Using quantities and Count out the first number and take away the second Children are encouraged objects, children to develop a mental number, e.g. 9-4= subtract two singlepicture of the number digit numbers and system in their heads to count on or back to use for calculation. find the answer. They should experience Subtract one-digit and practical calculation two-digit numbers to opportunities using a wide 20, including zero variety of practical (using concrete equipment, including small objects and pictorial world play, role play, representations). counters, cubes etc. Subtract numbers Those who are ready can using concrete objects, then begin to record pictorial their answers, e.g. 9-4=5. representations, and mentally, including: a Children will continue to two-digit number and ones; a two-digit use practical equipment number and tens; two and taking away two-digit numbers. strategies. To avoid the need to exchange for subtraction at this stage, it is advisable to continue to use equipment such as counters, cubes and the units from the Base 10 equipment, but not the tens, e.g. 13 - 4.



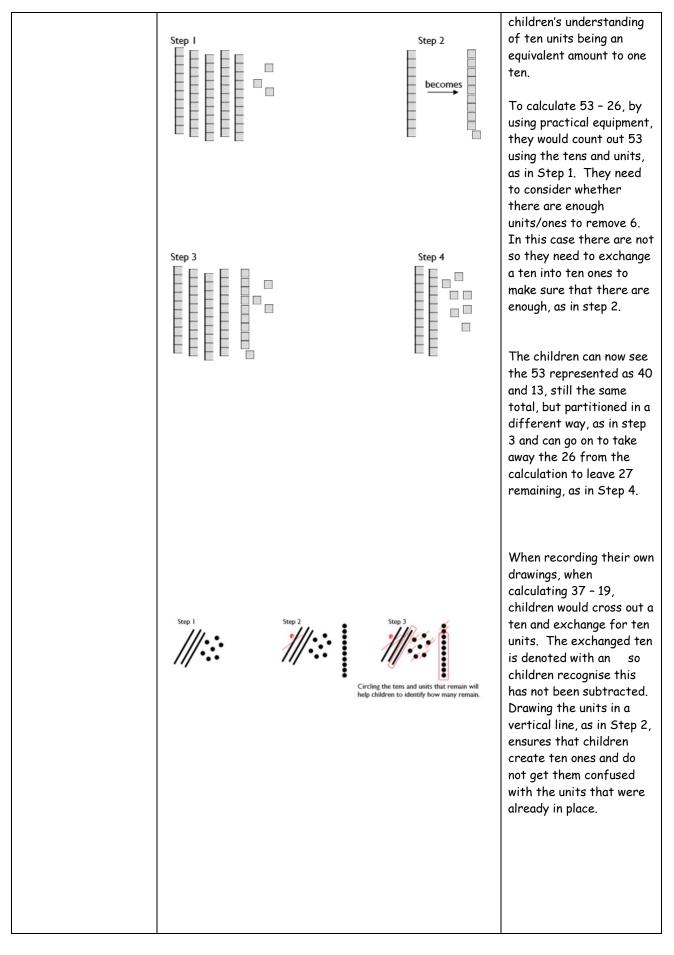


required. This relies on













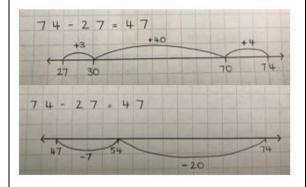
Subtract numbers with up to three digits, using formal written method of columnar subtraction.

Subtract numbers with up to 4 digits and decimals with one decimal place using the formal written method of columnar subtraction where appropriate.

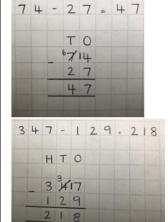
Subtract whole numbers with more than 4 digits and decimals with two decimal places, including formal written methods (columnar subtraction).

Subtract whole numbers and decimals using formal written methods (columnar subtraction).

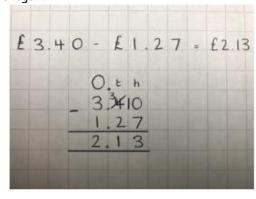
Stage 1



Stage 2



Stage 4



Subtraction starts with adding on using a numbered number line (jumps above the number line) or taking away on using a numbered number line (jumps below the number line) using mental 'counting on' strategies such as number bonds. This is a strategy which supports mental arithmetic.

A similar method is used to develop this stage but on a blank number line. This method relies on the children's knowledge of place value and mental subtraction strategies.

Stage 2 is the next stage of subtraction with use of exchanging which relies heavily on the mental strategies of subtraction multiples of 10 and 100.

Stage 3 is the final stage of subtraction where multiple use of exchanging is required.





Multiplication

Multiplication

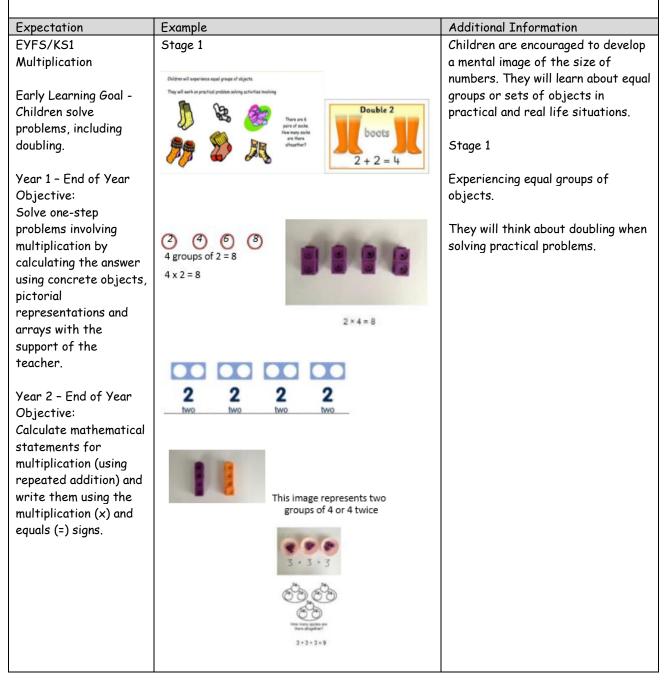
In developing a written method for multiplication, it is important that children understand the concept of multiplication, in that it is:

· repeated addition

They should also be familiar with the fact that it can be represented as an array

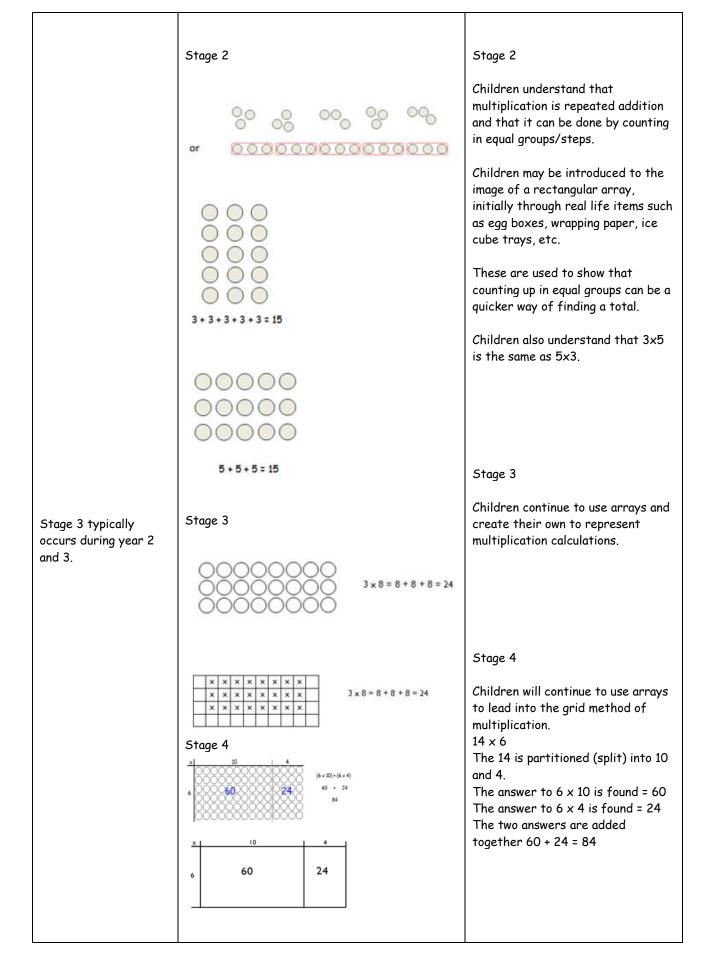
They also need to understand and work with certain principles, i.e. that it is:

- the inverse of division
- commutative i.e. 5×3 is the same as 3×5
- associative i.e. $2 \times 3 \times 5$ is the same as $2 \times (3 \times 5)$













KS2 Multiplication

Year 3 - End of Year
Objective:
Write and calculate
mathematical
statements for
multiplication using the
multiplication tables
that they know,
including for two-digit
numbers times onedigit numbers,
progressing to formal
written methods.*

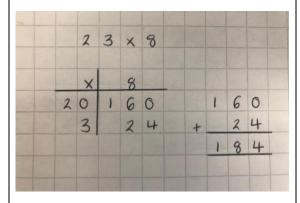
Year 4 - End of Year Objective: Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.

Year 5 - End of Year Objective: Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for twodigit numbers.

Year 6 - End of Year Objective: Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.

Multiply one-digit numbers with up to two decimal places by whole numbers.

Stage 1 (year 3)



		3	4	6	×	9						
		X		9								
3	0	0	2	7	0	0		2	7	0	0	
	4	0		3	6	0			3	6	0	
		6			5	4	+			5	4	
								3	1	1	4	
								1	x			ã

Stage 3i (year 4)

		3	6	8	×	6							
		X		6									
3	0	0	1	8	0	0			1	8	0	0	
	6	0		3	6	0				3		0	
		8			4	8					4	8	
									2	2	0	8	
									1	*			
		Th	H	T	U								
			3	6	8								
	×				6								
				4	8	(8	×	6	1			
			3	6	0	(6	0	×	6)		
	+	1	8	0	0	1	3	0	0	X	6)	
		2	2	0	8								

Stage 3ii

Stage 1 would start in Year 3 and stage 4 would typically appear in Year 6.

Multiplication starts with multiplying a single digit by a two digit number using grid method with awareness of place value.

It is made up of two stages; the multiplication stage and then column addition to get the final answer.

The same method is used to multiply single digits by three digit numbers and decimals

Stage 4 is an additional stage to our policy with the hope it will help children to understand to method needed when multiplying two digit numbers by three or four digit numbers. With the method clearly showing the stages of multiplying the ones and then the tens it allows them to understand the following

342 x 45 is broken down as:

300 x 5

40 x 5

2 x 5

and then

 300×40

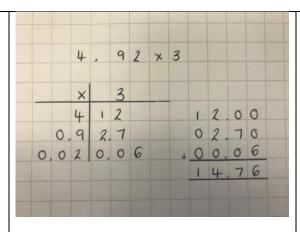
 42×40

2 x 40

Stage 5 is the final stage of multiplication using the formal written method where the children will require secure knowledge of multiplying numbers by ten and column addition with exchanging where appropriate

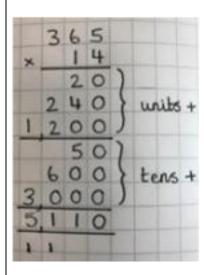






Stage 4





Stage 5



Division

Division





In developing a written method for division, it is important that children understand the concept of division, in that it is:

• repeated subtraction

They also need to understand and work with certain principles, i.e. that it is:

- the inverse of multiplication
- not commutative i.e. 15 ÷3 is not the same as 3 ÷ 15
- not associative i.e. $30 \div (5 \div 2)$ is not the same as $(30 \div 5) \div 2$

KS1 Division

Early Learning Goal: Children solve problems, including halving and sharing.

Year 1 - End of Year Objective:
Solve one-step problems involving division by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Year 2 - End of Year Objective: Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs.

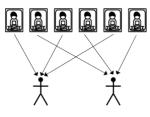
Stage 1







Stage 2







Children are encouraged to develop a mental image of the number system in their heads to use for calculation. They should experience practical calculation opportunities involving equal groups and equal sharing.

Stage 1

They may develop ways of recording calculations using pictures.

A child's jotting showing halving six spots between two sides of a ladybird.

A child's jotting showing how they shared the apples at snack time between two groups.

Stage 2

Children explore practical contexts where they share equally and group equally. 6 ÷ 2 = ?
Equal sharing (6 shared equally between 2)

6 football stickers are shared equally between 2 people, how many do they each get? Children may solve this by using a 'one for you, one for me' strategy until all of the stickers have been given out.

Stage 3



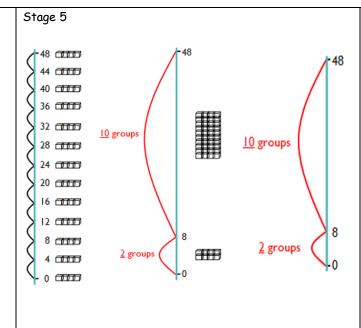


Equal grouping (How

many groups of 2 are 00000000000 there in 6?) There are 6 football stickers, how many people can have 2 stickers each? 0000000000 Stage 3 Children continue to use practical equipment to represent division calculations as grouping (repeated subtraction) and use jottings to support their calculation. 12 ÷ 3 = ? Children begin to read this calculation as, 'How many groups of 3 are there in 12?' At this stage, children will also be introduced to division calculations that result in remainders. Year 3 $13 \div 4 = 3$ remainder 1 Stage 4 Stage 4 43 ÷ 8 $43 \div 8 = 5$ remainder 3 At this stage, children also learn if the remainder should be rounded up or down e.g. 62 ÷ 8 = 7 remainder 6 I have 62p. Sweets are 8p each. How many can I buy? Answer: 7 (the remaining 6p is not enough for another sweet) Apples are packed into boxes of 8. There are 62







apples. How many boxes do I need?
Answer: 8 (the remaining 6 apples still need to be placed into a box).

Stage 5

The previous method of repeated subtraction on a number line is continued, but using a vertical number line alongside practical equipment. The repeated subtraction is made more efficient by subtracting 'chunks' of the divisor.

KS2 Division

Year 3 - End of Year Objective: Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers divided by one-digit numbers, progressing to formal written methods.*

Year 4 - End of Year Objective:
Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

Year 5 - End of Year Objective: Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and

Stage 6

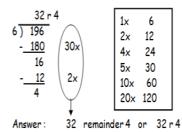
72 ÷ 3 3) 72 2x 6 Children should write 10× 5x 15 key facts in a menu 42 10x 30 box. This will help 10x them in identifying 12 the largest group they can subtract in 6 one chunk. Answer:

Stage 6

This is the 'chunking' method of division in which children use key facts of the multiplication tables of the divisor.

Stage 7

196 ÷ 6



The key facts in the menu box should be extended to include 4x and 20x.

Stage 7

During this stage children should become more efficient when using the chunking method by not having any subtraction steps that repeat a previous step. For example, when performing 196 ÷ 6 an initial subtraction of 60 (10×6) and two further subtractions of 60 (10 x 6 each) should be changed to a single subtraction of 180 (30 \times 6).





interpret remainders appropriately for the context.

Year 6 - End of Year
Objective:
Divide numbers up to 4
digits by a two-digit
number using the
formal written method
of short division where
appropriate,
interpreting
remainders according
to the context.

Use written division methods in cases where the answer has up to two decimal places.

Stage 7 Continued

972 ÷ 36

Answer: